

WHAT IS CLAIMED IS:

1 1. A system for adding an interference-resistant,
2 inaudible code to an audio signal comprising:
3 a sampler arranged to sample the audio signal at a
4 sampling rate and to generate therefrom a plurality of short
5 blocks of sampled audio, each of the short blocks having a
6 duration less than a minimum audibly perceivable signal delay;
7 a processor arranged to combine the plurality of short
8 blocks into a long block having a predetermined minimum duration;
9 a frequency transformation arranged to transform the
10 long block into a frequency domain signal comprising a plurality
11 of independently modulatable frequency indices, wherein a fre-
12 quency difference between two adjacent ones of the indices is
13 determined by the minimum duration and the sampling rate;
14 a frequency selector arranged to select a neighborhood
15 of frequency indices so that the frequency difference between a
16 lowest index and a highest index within the neighborhood is less
17 than a predetermined value; and,
18 an encoder arranged to modulate two or more of the
19 indices in the neighborhood so as to make a selected one of the

20 indices an extremum while keeping the total energy of the neigh-
21 borhood constant.

1 2. The system of claim 1 wherein the processor com-
2 prises a digital computer having a buffer memory.

1 3. The system of claim 1 wherein the frequency trans-
2 formation comprises a Fast Fourier Transform algorithm.

1 4. The system of claim 1 wherein the encoder comprises
2 an algorithm that increases the energy of a selected index in the
3 neighborhood and that decreases the energy of a short block
4 associated therewith.

5 5. A method of adding a code to a frequency band of a
6 sampled audio portion of a composite signal without thereby
7 introducing a perceptible delay between the encoded audio portion
8 and another portion of the composite signal, the method compris-
ing the steps of:

6 a) selecting a sampling rate and a frequency difference
7 between adjacent ones of a predetermined number of frequency
8 indices included in a frequency neighborhood;

9 b) determining from the sampling rate and from the
10 frequency difference a duration of a block of samples;
11 c) determining an integral number of sequential sub-
12 blocks to make up the block, where the integral number is se-
13 lected so that each of the sub-blocks has a sub-block duration
14 less than the perceptible delay; and,
15 d) processing the block so as to modulate a selected
16 one of the frequency indices without changing a total signal
17 energy of the band.

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4 synchronization block followed by a predetermined number of data
5 blocks, the apparatus comprising:

6 a buffer memory arranged to hold one of the blocks;

7 a frequency transformation arranged to transform the

8 one block into spectral data spanning a predetermined number of

9 frequency bands, wherein each of the frequency bands comprises a

10 respective neighborhood of frequency indices;

11 a processor arranged to determine, for each of the

12 neighborhoods, if a respective predetermined one of the frequency

13 indices is modulated; and,

14 a vote determiner arranged to determine that the one

15 block is the synchronization block if, in a majority of the

16 frequency bands, the respective modulated frequency index is a

17 respective index selected for inclusion in the synchronization

18 block;

19 wherein the processor is further arranged to determine

20 if, in one of the data blocks received subsequent to the synchro-

21 nization block, a respective predetermined one of the frequency

22 indices is modulated;

23 wherein the vote determiner is further arranged to

24 determine if, in a majority of the frequency bands, the respec-

25 tive modulated frequency index is a respective index selected for
26 inclusion in the one data block.

1 9. The apparatus of claim 8 wherein the frequency
2 transformation comprises a Fast Fourier Transform algorithm
3 executed by a digital computer.

1 10. The apparatus of claim 8 wherein the processor
2 comprises a general purpose digital computer operating under
3 program control and having a plurality of algorithms stored in a
4 memory.

1 11. The apparatus of claim 8 wherein the vote deter-
2 miner comprises an algorithm executed by a digital computer.

1 12. A method of reading a code from an audio signal by
2 sequentially transforming a sequence of blocks of audio samples
3 into spectral data spanning a predetermined number of frequency
4 bands, wherein each of the frequency bands comprises a predeter-
5 mined number of frequency indices, wherein each of the blocks
6 comprises a predetermined number of the samples, and wherein the

7 code comprises a synchronization block followed by a predeter-
8 mined number of data blocks, the method comprising the steps of:

9 a) determining, in each of the frequency bands of one
10 of the blocks of audio samples, if one of the frequency indices
11 is modulated;

12 b) comparing each modulated frequency index found in
13 step a) with that index selected for modulation in the respective
14 frequency band of the synchronization block;

15 c) determining that the one block is the synchroniza-
16 tion block if the majority of the comparisons made in step b)
17 result in a match, and otherwise repeating steps a) through b);

18 d) determining, in each of the frequency bands of one
19 of the data blocks received subsequent to the synchronization
20 block, if a respective one of the frequency indices is modulated;
21 and,

22 e) comparing the respective modulated frequency indices
23 found in step d) with ones of a plurality of predetermined index
24 patterns, each of the index patterns uniquely associated with a
25 respective code bit, and reading the code bit only if the major-
26 ity of modulated indices match the predetermined index pattern.

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1 13. The method of claim 12 wherein a value of k is
2 read as the code bit in step e) if the kth index in each of the
3 bands is modulated.

1 14. The method of claim 12 wherein the predetermined
2 index pattern comprises a pseudo-random sequence.

1 15. A system for adding an inaudible code to a tone-
2 like audio portion of a composite signal having two or more
3 portions, the system comprising:

4 a sampling apparatus arranged to sample audio at a
5 sampling rate and to generate therefrom a plurality of short
6 blocks of sampled audio, each of the short blocks having a
7 duration less than a minimum audibly perceptible signal delay;
8 a processor arranged to combine the plurality of short
9 blocks into a long block having a predetermined minimum duration;

10 a frequency transformation arranged to transform the
11 long block into a frequency domain signal comprising a plurality
12 of independently modulatable frequency indices located in a
13 plurality of frequency bands;

14 an encoder arranged to modulate two or more of the
15 indices in each of the frequency bands so as to make a respective

16 selected one of the indices an extremum while keeping a total
17 acoustic energy of the audio constant;
18 a signal analyzer arranged to determine if the tone-
19 like audio portion has a tone-like character within any one of
20 the predetermined number of neighborhoods; and,
21 an encoder suspender arranged to suspend the encoding
22 of the encoder within any neighborhood in which the tone-like
23 audio portion has a tone-like character.

16. The system of claim 15 wherein the audio signal is
part of a television broadcast signal.

17. The system of claim 15 wherein the frequency
transformation comprises a Fast Fourier Transform algorithm.

1 18. The system of claim 16 wherein the signal analyzer
2 comprises a computer arranged to carry out a masking algorithm
3 described in ISO/IEC 13818-7:1997.

1 19. A method for adding an inaudible code to at least
2 one of a predetermined number of frequency neighborhoods within a

3 tone-like audio portion of a composite signal having one or more
4 additional portions, the method comprising the steps of:

5 a) sampling the audio portion and generating from the
6 sampled signal a plurality of short blocks, each of the short
7 blocks having a duration less than a minimum audibly perceptible
8 signal delay;

9 b) combining the plurality of short blocks into a long
10 block having a predetermined minimum duration;

11 c) transforming the long block into a frequency domain
12 signal comprising a plurality of independently modulatable
13 frequency indices;

14 d) identifying those neighborhoods, if any, of the
15 predetermined number of frequency neighborhoods in which the
16 tone-like audio portion has a tone-like character; and,

17 e) modulating a respective index in each neighborhood
18 not identified in step d) so as to make a selected index in such
19 neighborhood an extremum while keeping the total acoustic energy
20 of the audio portion constant, and not modulating an index in any
21 of those neighborhoods identified in step d).

1 20. The method of claim 19 wherein the composite
2 signal comprises a television broadcast signal and wherein one of
3 the additional portions comprises a video signal.

1 *Sh* 21. The method of claim 19 wherein step c) comprises
2 the step of transforming the long block according to a Fast
3 Fourier Transform.

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10 a decoder having an input from the receiver, the
11 decoder arranged to acquire a respective test value of the code
12 bit from each of the frequency bands, to compare the test values,
13 to determine that one of the test values is the code bit only if
14 that test value is acquired from a majority of the frequency
15 bands, and to otherwise determine that no code bit has been read.

1 24. The broadcast audience measurement system of claim
2 23 wherein the audio signal is part of a television broadcast
3 signal.
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1 25. The broadcast audience measurement system of claim
2 23 wherein the receiver includes a microphone.
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1 26. The broadcast audience measurement system of claim
2 23 wherein the receiver comprises an audio output jack.
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1 27. A broadcast audience measurement system in which
2 an inaudible code added to an audio signal is read within a
3 statistically sampled dwelling unit, the system comprising:
4 an encoding apparatus arranged to add a code bit to a
5 sampled long block of the audio signal, the long block comprising

6 a predetermined number of short blocks, each of the short blocks
7 having a predetermined duration that is selected to be short
8 enough not to be perceptible to a member of a broadcast audience,
9 the encoding apparatus being further arranged to modulate a
10 selected frequency index in each of a plurality of frequency
11 neighborhoods so as to make each selected index an extremum in
12 the respective neighborhood thereof while keeping a total energy
13 of the audio signal constant;

14 a receiver within the dwelling, the receiver being
15 arranged to acquire the encoded audio signal; and,

16 a decoder arranged to read the code from the audio
17 signal, the decoder having an input from the receiver, the
18 decoder comprising a buffer memory arranged to store one of the
19 short blocks, the buffer memory being arranged to store a long
20 block.

1 28. The broadcast audience system of claim 27 wherein
2 the audio signal is part of a television signal.

1 29. The broadcast audience system of claim 27 wherein
2 the encoder comprises a frequency transformation arranged to
3 transform the long block into a frequency domain signal.

1 30. The broadcast audience system of claim 27 wherein
2 the receiver comprises a microphone.

1 31. The broadcast audience system of claim 27 wherein
2 the receiver comprises an audio output jack.

1 32. A method of encoding an audio signal comprising
2 the following steps:

3 a) generating a plurality of short blocks from the
4 audio signal, wherein each of the short blocks has a duration
5 less than a minimum audibly perceivable signal delay;

6 b) combining the plurality of short blocks into a long
7 block;

8 c) transforming the long block into a spectrum compris-
9 ing a plurality of independently modulatable frequency indices;
10 and,

11 d) modulating at least two of the indices so as to make
12 one of the indices an extremum while keeping the total energy of
13 a neighborhood of the modulated indices substantially constant.

1 33. A method of reading a code element from an audio
2 signal comprising the following steps:

3 a) transforming at least a portion of the audio signal
4 into spectral data spanning a predetermined number of frequency
5 bands having a plurality of frequency neighborhoods;

6 b) determining, for each of the neighborhoods, if one
7 of the frequency indices is modulated; and,

8 c) assigning a transmitted code value to the code
9 element if, in a majority of the neighborhoods, the respective
10 modulated frequency index is an index selected for inclusion in
11 the audio signal.